

Name: _____

Honors Calculus Summer Packet

Due: First day of school. Must show all work on a separate piece of paper.

Factor.

1. $8x^3 + 125$	2. $250x^4 + 128x$	3. $x^3 - 216y^3$
4. $35x^2y - 5x^2 - 56y + 8$	5. $5x^3 - 10x^2 - 3x + 6$	6. $15x^2 - 27x - 6$
7. $7x^2 - 44x + 12$	8. $6x^2 - 30x - 300$	9. $36x^2 - 49y^2$

Solve.

10. $2x^2 + 6x = -9$

Apply the remainder theorem to evaluate.

11. $f(x) = x^5 - 47x^3 - 16x^2 + 8x + 52$ at $x = 7$	12. $f(x) = x^4 - 3x^3 - 17x^2 + 2x - 7$ at $x = 3$
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Divide using long division.

13. $2x^4 + x^2 - 3x + 7 \div x + 2$	14. $3x^6 + 2x + 5 \div x - 1$
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Simplify.

15. $\frac{5}{n+5} + \frac{4n}{2n+6}$	16. $\frac{\frac{25}{4}}{\frac{1}{5} - \frac{4}{25}}$
17. $\frac{5-x}{x^2-25}$	18. $\left(4a^{\frac{5}{3}}\right)^{\frac{3}{2}}$
19. Let $f(x) = 2x + 1$ and $g(x) = 2x^2 - 1$. Find $g(f(m+2))$.	20. Find the domain of each function. a) $f(x) = x^2 - 6x$ b) $f(x) = \sin x$ c) $f(x) = \frac{1}{5-x}$ d) $f(x) = \sqrt{4-x}$ e) $f(x) = \frac{x}{x^2+3x+2}$

Simplify using the GCF.

21. $3x^2(2x^3 + 2)^{-3} - 6x(2x^3 + 2)^{-4}$	22. $-6\pi x^2(2x^2 - 1)^{-3/2} + 3\pi(2x^2 - 1)^{-1/2}$
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Solve for x on the interval from $[0, 2\pi]$

23. $\sin x + 2 = 3$	24. $\cos x + \sqrt{3} = -\cos x$
25. $4 \sin^2 \theta - 3 = 0$	26. $2 \sin^2 x - 3 \sin x + 1 = 0$

Verify the following trig identities.

27. $\frac{\tan^2 x}{\tan^2 x + 1} = \sin^2 x$	28. $\sin^4 x - \cos^4 x = 1 - 2 \cos^2 x$
29. $(\sec^2 x - 1) \cos^2 x = \sin^2 x$	30. $\sin \theta - \sin \theta \cos^2 \theta = \sin^3 \theta$

Must know!

Reciprocal Identities

$$\csc(\theta) = \frac{1}{\sin(\theta)}$$

$$\sin(\theta) = \frac{1}{\csc(\theta)}$$

$$\sec(\theta) = \frac{1}{\cos(\theta)}$$

$$\cos(\theta) = \frac{1}{\sec(\theta)}$$

$$\cot(\theta) = \frac{1}{\tan(\theta)}$$

$$\tan(\theta) = \frac{1}{\cot(\theta)}$$

